A Guided Tour of CML, the Coded Modulation Library

last updated on Feb. 24, 2008

Matthew Valenti Iterative Solutions and West Virginia University Morgantown, WV 26506-6109 mvalenti@wvu.edu

Outline

- 1. CML overview
 - What is it? How to set it up and get started?
- 2. Uncoded modulation
 - Simulate uncoded BPSK and QAM in AWGN and Rayleigh fading
- 3. Coded modulation
 - Simulate a turbo code from UMTS 25.212
- 4. Ergodic (Shannon) capacity analysis
 - Determine the modulation constrained capacity of BPSK and QAM
- 5. Outage analysis
 - Determine the outage probability over block fading channels.
 - Determine the outage probability of finite-length codes
- 6. The internals of CML
- 7. Throughput calculation
 - Convert BLER to throughput for hybrid-ARQ



What is CML?

- CML is an open source toolbox for simulating capacity approaching codes in Matlab.
- Available for free at the **Iterative Solutions** website:
 - www.iterativesolutions.com
- Runs in matlab, but uses c-mex for efficiency.
- First release was in Oct. 2005.
 - Used code that has been developed starting in 1996.

Features

Simulation of BICM (bit interleaved coded modulation)

- Turbo, LDPC, or convolutional codes.
- PSK, QAM, FSK modulation.
- BICM-ID: Iterative demodulation and decoding.
- Generation of ergodic capacity curves
 - BICM/CM constrained modulation.
- Information outage probability
 - Block fading channels.
 - Blocklength-constrained channels (AWGN or fading)
- Calculation of throughput of hybrid-ARQ.

Supported Standards

- Binary turbo codes:
 - UMTS/3GPP, including HSDPA and LTE.
 - cdma2000/3GPP2.
 - CCSDS.
 - Duobinary turbo codes:
 - DVB-RCS.
 - WiMAX IEEE 802.16.
- LDPC codes:
 - DVB-S2.
 - Mobile WiMAX IEEE 802.16e.

Simulation Data is Valuable

- CML saves simulation state frequently
 - parameter called "save_rate" can be tuned to desired value.
- CML can be stopped at any time.
 - Intentionally: Hit CTRL-C within matlab.
 - Unintentionally: Power failure, reboot, etc.
- CML automatically resumes simulation
 - If a simulation is run again, it will pickup where it left off.
 - Can reset simulation by setting "reset=1".
 - SNR points can be added or deleted prior to restarting.
- Simulations can be made more confident by requesting additional trials prior to restarting.
 - The new results will be added to the old ones.

Compiled Mode

- A flag called "compiled_mode" can be used to run CML independently of matlab.
- CML must first be compiled using the matlab compiler.
- Advantages:
 - Can run on machines without matlab.
 - Can run on a grid computer.

WebCML

- WebCML is a new initiative sponsored by NASA and NSF.
- Idea is to upload simulation parameters to a website and hit a "simulate" button.
 - Simulation begins on the webserver.
 - The webserver will divide the simulation into multiple jobs which are sent to a grid computer.
- Results can be retrieved while simulation is running and once it has completed.
- The grid is comprised of ordinary desktop computers.
 - The grid compute engine is a screen saver.
 - Kicks in only when computer is idle.
 - Users of WebCML are encouraged to donate their organizations computers to the grid.

Getting Started with CML

Download

- www.iterativesolutions.com/download.htm
- Unzip into a directory
 - Root directory will be ./cml
- About simulation databases
 - A large database of previous simulation results can be downloaded.
 - Unzip each database and place each extracted directory into the ./cml/output directory
- About c-mex files.
 - C-mex files are compiled for PC computers.
 - For unix and mac computers, must compile.
 - Within matlab, cd to ./cml/source and type "make".

Starting and Interacting with CML

- Launch matlab
- Cd to the ./cml directory
- Type "CmlStartup"
 - This sets up paths and determines the version of matlab.
- To run CML, only two functions are needed:
 - CmlSimulate
 - Runs one or more simulations.
 - Simulation parameters are stored in text files.
 - Currently .m scripts, to be changed to XML files soon.
 - The argument tells CML which simulation(s) to run.
 - CmIPlot
 - Plots the results of one or more simulations.

Scenario Files

and the SimParam Structure

- The parameters associated with a set of simulations is stored in a scenario file.
 - Located in one of two directories
 - ./cml/scenarios for publicly available scenarios
 - ./cml/localscenarios for personal user scenarios
 - Other directories could be used if they are on the matlab path.
 - .m extension.
- Exercise
 - Edit the example scenario file: UncodedScenarios.m
- The main content of the scenario file is a structure called sim_param
 - Sim_param is an array.
 - Each element of the array is called a *record* and corresponds to a single distinct simulation.

Common Parameters

- List of all parameters can be found in:
 - ./cml/mat/DefineStructures.m
 - ./cml/documentation/readme.pdf
- Default values are in the DefineStructures.m file
- Some parameters can be changed between runs, others cannot.
 - sim_param_changeable
 - sim_param_unchangeable

Dissecting the SimParam Structure: The simulation type

- sim_param(record).sim_type =
 - 'uncoded'
 - BER and SER of uncoded modulation
 - 'coded'
 - BER and FER of coded modulation
 - 'capacity'
 - The Shannon capacity under modulation constraints.
 - 'outage'
 - The information outage probability of block fading channels
 - Assumes codewords are infinite in length
 - 'bloutage'
 - Information outage probability in AWGN or ergodic/block fading channels
 - Takes into account lenth of the code.
 - 'throughput'
 - By using FER curves, determines throughput of hybrid ARQ
 - This is an example of an *analysis* function ... no simulation involved.

Lesser Used Simulation Types

- sim_param(record).sim_type =
 - 'bwcapacity'
 - Shannon capacity of CPFSK under bandwidth constraints.
 - 'minSNRvsB'
 - Capacity limit of CPFSK as a function of bandwidth

Parameters Common to All Simulations

- Sim_param(record).
 - comment = {string}
 - Text, can be anything.
 - legend = {string}
 - What to put in figure caption
 - linetype = {string}
 - Color, type, and marker of line. Uses syntax from matlab "plot".
 - filename = {string}
 - Where to save the results of the simulation
 - Once filename is changed, any parameter can be changed.
 - reset = {0,1} with default of 0
 - Indication to resume "0" or restart "1" simulation when run again.
 - If reset = 1, any parameter may be changed.

Specifying the Simulation

sim_param(record).

- SNR = {vector}
 - Vector containing SNR points in dB
 - Can add or remove SNR points between runs
- SNR_type = {'Eb/No in dB' or 'Es/No in dB'}
 - For some simulation types, only one option is supported.
 - E.g. for *capacity* simulations, it must be Es/No
- save_rate = {scalar integer}
 - · An integer specifying how often the state of the simulation is saved
 - Number of trials between saves.
 - Simulation echoes a period '.' every time it saves.

Specifying the Simulation (cont'd)

sim_param(record).

- max_trials = {vector}
 - A vector of integers, one for each SNR point
 - Tells simulation maximum number of trials to run per point.
- max_frame_errors = {vector}
 - Also a vector of integers, one for each SNR point.
 - Tells simulation maximum number of frame errors to log per point.
 - Simulation echoes a 'x' every time it logs a frame error.
- minBER = {scalar}
 - Simulation halts once this BER is reached
- minFER = {scalar}
 - Simulation halts once this FER is reached.

Outline

- 1. CML overview
 - What is it? How to set it up and get started?
- 2. Uncoded modulation
 - Simulate uncoded BPSK and QAM in AWGN and Rayleigh fading
- 3. Coded modulation
 - Simulate a turbo code from UMTS 25.212
- 4. Ergodic (Shannon) capacity analysis
 - Determine the modulation constrained capacity of BPSK and QAM
- 5. Outage analysis
 - Determine the outage probability over block fading channels.
 - Determine the outage probability of finite-length codes
- 6. The internals of CML
- 7. Throughput calculation
 - Convert BLER to throughput for hybrid-ARQ

Specifying Modulation

- sim_param(record).
 - modulation = {string}
 - Specifies the modulation type
 - May be 'BPSK', 'QPSK', 'QAM', 'PSK', 'APSK', 'HEX', or 'FSK'
 - 'HSDPA' used to indicate QPSK and QAM used in HSDPA.
 - All but FSK are 2 dimensional modulations
 - Uses a complex scalar value for each symbol.
 - Default is 'BPSK'
 - New (version 1.9 and above): Can also be set to "custom".
 - mod_order = {integer scalar}
 - Number of points in the constellation.
 - Power of 2.
 - Default is 2.
 - In some cases, M=0 is used to indicate an unconstrained Gaussian input.
 - S_matrix = {complex vector}
 - Only used for "custom" modulation type.
 - A vector of length "mod_order" containing the values of the symbols in the signal set S.

Specifying Modulation

- sim_param(record).
 - mapping = {integer vector}
 - A vector of length M specifying how data bits are mapped to symbols.
 - Vector contains the integers 0 through M-1 exactly once.
 - ith element of vector is the set of bits associated with the ith symbol.
 - · Alternatively, can be a string describing the modulation, like 'gray' or 'sp'
 - Default is 'gray'
 - framesize = {integer scalar}
 - The number of symbols per Monte Carlo trial
 - For coded systems, this is number of bits per codeword
 - demod_type = {integer scalar}
 - A flag indicating how to implement the demodulator
 - 0 = log-MAP (approximated linearly)
 - 1 = max-log-MAP
 - 2 = constant-log-MAP
 - 3 and 4 other implementations of log-MAP
 - Max-log-MAP is fastest.
 - Does not effect the uncoded error rate.
 - However, effects coded performance

M-ary Complex Modulation

- μ = log₂ M bits are mapped to the symbol x_k, which is chosen from the set S = {x₁, x₂, ..., x_M}
 - The symbol is multidimensional.
 - 2-D Examples: QPSK, M-PSK, QAM, APSK, HEX
 - These 2-D signals take on complex values.
 - M-D Example: FSK
 - FSK signals are represented by the M-dimensional complex vector **X**.
- The signal $y = hx_k + n$ is received
 - h is a complex fading coefficient (scalar valued).
 - n is complex-valued AWGN noise sample
 - More generally (FSK), $\mathbf{Y} = \mathbf{h} \mathbf{X} + \mathbf{N}$
 - Flat-fading: All FSK tones multiplied by the same fading coefficient h.
- Modulation implementation in CML
 - The complex signal set S is created with the CreateConstellation function.
 - Modulation is performed using the Modulate function.

Log-likelihood of Received Symbols

- Let p(x_k|y) denote the probability that signal x_k ∈S was transmitted given that y was received.
- Let f(x_k|y) = K p(x_k|y), where K is any multiplicative term that is constant for all x_k.
- When all symbols are equally likely, $f(\mathbf{x}_k | \mathbf{y}) \propto f(\mathbf{y} | \mathbf{x}_k)$
- For each signal in S, the receiver computes $f(\mathbf{y}|\mathbf{x}_k)$
 - This function depends on the modulation, channel, and receiver.
 - Implemented by the **Demod2D** and **DemodFSK** functions, which actually computes log $f(\mathbf{y}|\mathbf{x}_k)$.
- Assuming that all symbols are equally likely, the most likely symbol x_k is found by making a hard decision on f(y|x_k) or log f(y|x_k).

Example: QAM over AWGN.

Let y = x + n, where n is complex i.i.d. N(0,N₀/2) and the average energy per symbol is E[|x|²] = E_s

$$p(y|x_k) = \frac{1}{2\pi\sigma^2} \exp\left\{\frac{-|y-x_k|^2}{2\sigma^2}\right\}$$
$$f(y|x_k) = \exp\left\{\frac{-|y-x_k|^2}{2\sigma^2}\right\}$$
$$\log f(y|x_k) = \frac{-|y-x_k|^2}{2\sigma^2}$$

$$=\frac{-E_{s}|y-x_{k}|^{2}}{N_{o}}$$

CML Overview

Converting symbol liklihoods to bit LLR



Log-domain Implementation

$$\begin{split} \lambda_{n} &= \log \frac{\sum_{X_{k} \in S_{n}^{(1)}} f\left(Y \mid X_{k}\right)}{\sum_{X_{k} \in S_{n}^{(0)}} f\left(Y \mid X_{k}\right)} \\ &= \log \sum_{X_{k} \in S_{n}^{(1)}} f\left(Y \mid X_{k}\right) - \log \sum_{X_{k} \in S_{n}^{(0)}} f\left(Y \mid X_{k}\right) \\ &= \max_{X_{k} \in S_{n}^{(1)}} \left\{ \log f\left(Y \mid X_{k}\right) \right\} - \max_{X_{k} \in S_{n}^{(0)}} \left\{ \log f\left(Y \mid X_{k}\right) \right\} \qquad \begin{array}{c} \log \operatorname{-MAP} \\ \operatorname{demod_type} = 0 \end{array} \\ &\approx \max_{X_{k} \in S_{n}^{(1)}} \left\{ \log f\left(Y \mid X_{k}\right) \right\} - \max_{X_{k} \in S_{n}^{(0)}} \left\{ \log f\left(Y \mid X_{k}\right) \right\} \qquad \begin{array}{c} \max_{d = \operatorname{MAP}} \\ \operatorname{demod_type} = 0 \end{array} \\ &\approx \max_{X_{k} \in S_{n}^{(1)}} \left\{ \log f\left(Y \mid X_{k}\right) \right\} - \max_{X_{k} \in S_{n}^{(0)}} \left\{ \log f\left(Y \mid X_{k}\right) \right\} \qquad \begin{array}{c} \max_{d = \operatorname{MAP}} \\ \operatorname{demod_type} = 1 \end{array} \end{split}$$

The max* function



y-x

FSK-Specific Parameters

sim_param(record).

- $-h = \{scalar\}$
 - The modulation index
 - h=1 is orthogonal
- csi_flag = {integer scalar}
 - 0 = coherent (only available when h=1)
 - 1 = noncoherent w/ perfect amplitudes
 - 2 = noncoherent without amplitude estimates

Specifying the Channel

- sim_param(record).
 - channel = {'AWGN', 'Rayleigh', 'block'}
 - 'Rayleigh' is "fully-interleaved" Rayleigh fading
 - 'block' is for coded simulation type only
 - blocks_per_frame = {scalar integer}
 - For block channel only.
 - Number of independent blocks per frame.
 - Block length is framesize/blocks_per_frame
 - bicm = {integer scalar}
 - 0 do not interleave bits prior to modulation
 - 1 interleave bits prior to modulation (default)
 - 2 interleave and perform iterative demodulation/decoding
 - This option is irrelevant unless a channel code is used

Exercises

- Create and run the following simulations:
 - BPSK in AWGN
 - 64QAM with gray labeling in AWGN
 - 64QAM with gray labeling in Rayleigh fading
 - Choices that need to be made?
 - Framesize?
 - Save_rate?
 - Min_BER?
 - Min_frame_errors?
 - Demod_type?
- Plot all the results on the same figure.

Outline

- 1. CML overview
 - What is it? How to set it up and get started?
- 2. Uncoded modulation
 - Simulate uncoded BPSK and QAM in AWGN and Rayleigh fading
- 3. Coded modulation
 - Simulate a turbo code from UMTS 25.212
- 4. Ergodic (Shannon) capacity analysis
 - Determine the modulation constrained capacity of BPSK and QAM
- 5. Outage analysis
 - Determine the outage probability over block fading channels.
 - Determine the outage probability of finite-length codes
- 6. The internals of CML
- 7. Throughput calculation
 - Convert BLER to throughput for hybrid-ARQ

Coded Systems: Code Configuration

- Only for sim_param(record).sim_type = 'coded'
- sim_param(record).code_configuration = {scalar int}
 - 0 = Convolutional
 - 1 = binary turbo code (PCCC)
 - 2 = LDPC
 - 3 = HSDPA turbo code
 - 4 = UMTS turbo code with rate matching
 - 5 = WiMAX duobinary tailbiting turbo code (CTC)
 - 6 = DVB-RCS duobinary tailbiting turbo code

Convolutional Codes

- Only rate 1/n mother codes supported.
 - Can puncture to higher rate.
- Code is always terminated by a tail.
 - Can puncture out the tail.
- sim_param(record).
 - g1 = {binary matrix}
 - Example: (133,171) code from Proakis

- 1 1 1 1 0 0 1];
- Constraint length = number of columns
- Rate 1/n where n is number of rows.
- nsc_flag1 = {scalar integer}
 - 0 for RSC
 - 1 for NSC
- Can handle cyclic block codes as a rate 1 terminated RSC code

Convolutional Codes: Decoding Algorithms



Punctured Convolutional Codes

- sim_param(record).
 - pun_pattern1 = {binary matrix}
 - Puncturing pattern
 - n rows
 - arbitrary number of columns (depends on puncture period)
 - 1 means keep bit, 0 puncture it.
 - number greater than 1 is number of times to repeat bit.
 - tail_pattern1 = {binary matrix}
 - tail can have its own puncturing pattern.

Turbo Codes

- sim_param(record).
 - Parameters for first constituent code
 - g1
 - nsc_flag1
 - pun_pattern1
 - tail_pattern1
 - Parameters for second constituent code
 - g2
 - nsc_flag2
 - pun_pattern2
 - tail_pattern2

Turbo Codes (cont'd)

- sim_param(record).
 - code_interleaver = {string}
 - A string containing the command used to generate the interleaver.
 - Examples include:
 - "CreateUmtsInterleaver(5114)" % UMTS interleaver.
 - "CreateLTEInterleaver(6144)" % LTS interleaver.
 - "CreateCCSDSInterleaver(8920)" % CCSDS interleaver.
 - "randperm(40)-1" % a random interleaver of length 40.
 - Can replace above lengths with other valid lengths.
 - decoder_type = {integer scalar}
 - Same options as for convolutional codes (except no Viterbi allowed).
 - max_iterations = {integer scalar}
 - Number of decoder iterations.
 - Decoder will automatically halt once codeword is correct.
 - plot_iterations = {integer scalar}
 - Which iterations to plot, in addition to max_iterations
UMTS Rate Matching

- sim_param(record)
 - framesize = {integer scalar}
 - number of data bits
 - code_bits_per_frame = {integer scalar}
 - number of code bits
- When code_configuration = 4, automatically determines rate matching parameters according to UMTS (25.212)

HSDPA Specific Parameters

- sim_param(record).
 - N_IR = {integer scalar}
 - Size of the virtual IR buffer
 - X_set = {integer vector}
 - Sequence of redundancy versions (one value per ARQ transmission)
 - P = {integer scalar}
 - Number of physical channels per turbo codeword
- Examples from HSET-6 TS 25.101

- QPSK
 - framesize = 6438
 - X_set = [0 2 5 6]
 - P = 5 (i.e. 10 physical channels used for 2 turbo codewords)
- 16-QAM
 - framesze = 9377
 - X_set = [6 2 1 5]
 - P = 4 (i.e. 8 physical channels used for 2 turbo codewords)

LDPC

- sim_parameters(record).
 - parity_check_matrix = {string}
 - A string used to generate the parity check matrix
 - decoder_type
 - 0 Sum-product (default)
 - 1 Min-sum
 - 2 Approximate-min-star
 - max_iterations
 - Number of decoder iterations.
 - Decoder will automatically halt once codeword is correct.
 - plot_iterations
 - Which iterations to plot, in addition to max_iterations

Block Fading

- For coded simulations, block fading is supported.
- Sim_param(record).channel = 'block'
- Sim_param(record).blocks_per_frame
 - The number of independent blocks per frame
- Example, HSDPA with independent retransmissions
 - blocks_per_frame = length(X_set);

Exercises

Simulate

- A convolutional code with g=(7,5) over AWGN with BPSK
- The same convolutional code punctured to rate 3/4.
- The UMTS turbo code with 16-QAM
 - Unpunctured w/ 640 input bits
 - Punctured to force the rate to be 1/2.
 - Compare log-MAP and max-log-MAP
- HSDPA
 - HSET-6
 - Quasi-static block fading

Outline

- 1. CML overview
 - What is it? How to set it up and get started?
- 2. Uncoded modulation
 - Simulate uncoded BPSK and QAM in AWGN and Rayleigh fading
- 3. Coded modulation
 - Simulate a turbo code from UMTS 25.212
- 4. Ergodic (Shannon) capacity analysis
 - Determine the modulation constrained capacity of BPSK and QAM
- 5. Outage analysis
 - Determine the outage probability over block fading channels.
 - Determine the outage probability of finite-length codes
- 6. The internals of CML
- 7. Throughput calculation
 - Convert BLER to throughput for hybrid-ARQ

Noisy Channel Coding Theorem (Shannon 1948)

Consider a memoryless channel with input X and output Y



- The channel is completely characterized by p(x,y)

The capacity C of the channel is

$$C = \max_{p(x)} \left\{ I(X;Y) \right\} = \max_{p(x)} \left\{ \iint p(x,y) \log \frac{p(x,y)}{p(x)p(y)} dx dy \right\}$$

- where I(X,Y) is the (average) *mutual information* between X and Y.

- The channel capacity is an upper bound on *information rate* r.
 - There exists a code of rate r < C that achieves reliable communications.
 - "Reliable" means an arbitrarily small error probability.

Capacity of the AWGN Channel with Unconstrained Input



Capacity of the AWGN Channel with a Modulation-Constrained Input Suppose X is drawn with equal probability from the finite set S = { $X_1, X_2, ..., X_M$ } Modulator: ML Receiver: Pick X_k at random from Compute $f(Y|X_k)$ for every $X_k \in S$ $S = \{X_1, X_2, ..., X_M\}$ N_k - where $f(Y|X_k) = \kappa p(Y|X_k)$ for any κ common to all X_k Since p(x) is now fixed $C = \max_{p(x)} \{I(X;Y)\} = I(X;Y)$ - i.e. calculating capacity boils down to calculating mutual info.

Entropy and Conditional Entropy



2/24/2008

Calculating Modulation-Constrained Capacity

To calculate:

I(X;Y) = H(X) - H(X | Y)We first need to compute H(X)

$$H(X) = E[h(X)]$$

= $E\left[\log \frac{1}{p(X)}\right]^{-1}$
= $E[\log M]$
= $\log M$

Next, we need to compute H(X|Y)=E[h(X|Y)]

- This is the "hard" part.
- In some cases, it can be done through numerical integration.
- Instead, let's use Monte Carlo simulation to compute it.

Step 1: Obtain p(x|y) from f(y|x)



Step 2: Calculate h(x|y)



2/24/2008

Step 3: Calculating H(X|Y)



Example: BPSK



BPSK Capacity as a Function of Number of Simulation Trials



Unconstrained vs. BPSK Constrained Capacity



Power Efficiency of Standard Binary Channel Codes







Capacity of Nonorthogonal CPFSK



BICM (Caire 1998)

- Coded modulation (CM) is required to attain the aforementioned capacity.
 - Channel coding and modulation handled jointly.
 - Alphabets of code and modulation are matched.
 - e.g. trellis coded modulation (Ungerboeck); coset codes (Forney)
- Most off-the-shelf capacity approaching codes are binary.
- A pragmatic system would use a binary code followed by a bitwise interleaver and an M-ary modulator.
 - Bit Interleaved Coded Modulation (BICM).



BICM Receiver



BICM Capacity



CM vs. BICM Capacity for 16QAM



BICM-ID (Li & Ritcey 1997)



CML Overview

 $X_k \in S_n^{(0)}$

2/24/2008

Capacity Simulations in CML

- sim_param(record).sim_type = 'capacity'
- Exact same parameters as for uncoded simulations
 - SNR
 - SNR_type = 'Es/No in dB'
 - framesize
 - modulation
 - mod_order
 - channel
 - bicm
 - demod_type
 - max_trials

Exercises

- Determine the capacity for
 - BPSK in AWGN
 - 64QAM with gray labeling in AWGN
 - 64QAM with gray labeling in Rayleigh fading
 - Setup BICM-ID for
 - 16-QAM with SP mapping in AWGN and (7,5) CC.

Outline

- 1. CML overview
 - What is it? How to set it up and get started?
- 2. Uncoded modulation
 - Simulate uncoded BPSK and QAM in AWGN and Rayleigh fading
- 3. Coded modulation
 - Simulate a turbo code from UMTS 25.212
- 4. Ergodic (Shannon) capacity analysis
 - Determine the modulation constrained capacity of BPSK and QAM
- 5. Outage analysis
 - Determine the outage probability over block fading channels.
 - Determine the outage probability of finite-length codes
- 6. The internals of CML
- 7. Throughput calculation
 - Convert BLER to throughput for hybrid-ARQ

Ergodicity vs. Block Fading

- Up until now, we have assumed that the channel is ergodic.
 - The observation window is large enough that the time-average converges to the statistical average.
- Often, the system might be *nonergodic*.
- Example: *Block fading*



CML Overview

Accumulating Mutual Information

- The SNR γ_{b} of block b is a random.
- Therefore, the mutual information I_b for the block is also random.
 - With a complex Gaussian input, $I_b = log(1+\gamma_b)$
 - Otherwise the modulation constrained capacity can be used for I_b



Information Outage

An *information outage* occurs after B blocks if

 $I_1^B < R$

- where R≤log₂M is the rate of the coded modulation
- An outage implies that no code can be reliable for the particular channel instantiation
- The information outage probability is

$$P_0 = P \Big[I_1^B < R \Big]$$

– This is a practical bound on FER for the actual system.



Outage Simulation Type

- sim_param(record).
 - blocks_per_frame
 - Assumes block fading channel
 - mod_order
 - 0 for Gaussian input case
 - rate
 - Code rate.
 - Outage whenever MI < rate
 - combining_type = {'code', 'diversity'}
 - input_filename
 - Required if mod_order > 0
 - Contains results of a capacity simulation.
 - Used for a table look-up operation

Finite Length Codeword Effects




Bloutage Simulation Type

- Set up like an uncoded simulation
 - framesize
 - specify the modulation
 - Set mod_order = 0 for unconstrained Gaussian input
 - specify the channel (AWGN, Rayleigh, etc.)
- Also requires the rate
- Saves FER, not BER

Outline

- 1. CML overview
 - What is it? How to set it up and get started?
- 2. Uncoded modulation
 - Simulate uncoded BPSK and QAM in AWGN and Rayleigh fading
- 3. Coded modulation
 - Simulate a turbo code from UMTS 25.212
- 4. Ergodic (Shannon) capacity analysis
 - Determine the modulation constrained capacity of BPSK and QAM
- 5. Outage analysis
 - Determine the outage probability over block fading channels.
 - Determine the outage probability of finite-length codes
- 6. The internals of CML
- 7. Throughput calculation
 - Convert BLER to throughput for hybrid-ARQ

Main Program Flow

CmlSimulate

- ReadScenario
 - Runs SingleRead for each record
 - Performs sanity check on sim_param structure
 - Initializes or restores the sim_state structure
- For each record~
 - SingleSimulate if a simulation
 - Otherwise, runs one of the analysis functions:
 - CalculateThroughput
 - CalculateMinSNR
 - CalculateMinSNRvsB

SingleSimulate

- Seeds random number generator
- Branches into
 - SimulateMod
 - For uncoded, coded, and bloutage
 - SimulateUGI
 - For a blocklength-constrained outage simulation with unconstrained Gaussian input.
 - SimulateCapacity
 - For capacity
 - SimulateOutage
 - For outage

SimulateMod

- Main subfunctions (coded/uncoded cases:
 - CmlEncode
 - CmlChannel
 - CmlDecode
- For bloutage, replace CmlDecode with
 - Somap
 - capacity

SimulateCapacity

- Operates like SimulateMod with sim_type = 'bloutage'
 - However, instead of comparing MI of each codeword against the rate, keeps a running average of MI.

SimulateOutage

- Randomly generates SNR for each block
- Performs table lookup to get MI from SNR
- Compares MI against threshold

Outline

- 1. CML overview
 - What is it? How to set it up and get started?
- 2. Uncoded modulation
 - Simulate uncoded BPSK and QAM in AWGN and Rayleigh fading
- 3. Coded modulation
 - Simulate a turbo code from UMTS 25.212
- 4. Ergodic (Shannon) capacity analysis
 - Determine the modulation constrained capacity of BPSK and QAM
- 5. Outage analysis
 - Determine the outage probability over block fading channels.
 - Determine the outage probability of finite-length codes
- 6. The internals of CML
- 7. Throughput calculation
 - Convert BLER to throughput for hybrid-ARQ

Hybrid-ARQ (Caire and Tunnineti 2001)

- Once $I_1^B > R$ the codeword can be decoded with high reliability.
- Therefore, why continue to transmit any more blocks?
- With hybrid-ARQ, the idea is to request retransmissions until $I_1^B > R$
 - With hybrid-ARQ, outages can be avoided.
 - The issue then becomes one of latency and throughput.



Latency and Throughput of Hybrid-ARQ

- With hybrid-ARQ B is now a random variable.
 - The average *latency* is proportional to E[B].
 - The average *throughput* is inversely proportional to E[B].
- Often, there is a practical upper limit on B
 - Rateless coding (e.g. Raptor codes) can allow $B_{max} \rightarrow \infty$
- An example
 - HSDPA: High-speed downlink packet access
 - 16-QAM and QPSK modulation
 - UMTS turbo code
 - HSET-1/2/3 from TS 25.101

$$-B_{max} = 4$$



Conclusions: Design Flow with CML

- When designing a system, first determine its capacity.
 - Only requires a slight modification of the modulation simulation.
 - Does not require the code to be simulated.
 - Allows for optimization with respect to free parameters.
- After optimizing with respect to capacity, design the code.
 - BICM with a good off-the-shelf code.
 - Optimize code with respect to the EXIT curve of the modulation.
- Information outage analysis can be used to characterize:
 - Performance in slow fading channels.
 - Delay and throughput of hybrid-ARQ retransmission protocols.
 - Finite codeword lengths.